

Basic statistical test of bit sequences

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Date/Time: 10.01.2013,18:13 hour

file: txor31.rnd size: 10240000 Bytes

Test of null-hypothesis:

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Bit stream ist a stream of truly randomly drawn number 0,1 with same probability p = 0.5

Non-overlapping byte count:

00	40336	39931	39764	39809	40107	39879	40157	40378
08	40248	40361	39881	39910	39831	39891	40005	39823
10	40152	40214	40056	39587	39719	39515	39719	39794
18	40246	40438	40020	39906	40047	40053	39994	39912
20	39932	40233	40032	39759	40066	40145	39638	40388
28	40120	40528	39787	39978	40167	39804	39773	39924
30	40150	40118	40098	39973	39893	39661	40020	39990
38	39957	40012	39538	39788	39457	39934	39737	40201
40	40063	39660	40047	39783	40202	40249	40030	39941
48	40118	39776	39987	40407	40423	39643	40329	40118
50	39965	39999	40072	40348	40233	40006	39927	39731
58	40023	40323	40107	39791	40246	40074	39695	39852
60	40229	40006	40157	40063	40256	40027	40401	40177
68	39939	39908	39778	39637	40113	39998	39783	40326
70	39927	40078	39989	39706	40174	39993	39584	40215
78	39739	39750	40005	40007	40027	39918	40000	39853
80	40025	39690	40201	39769	40133	39985	39851	39934
88	40048	39920	40086	39860	39832	40062	39936	39794
90	40318	39896	40259	40136	40032	39848	40071	39969
98	39854	40090	40254	39636	39872	40396	40109	40288
a0	40170	40114	39943	39948	40227	40045	40087	39839
a8	39900	39793	39897	39870	39963	39841	40249	39932
b0	39963	39837	39984	40159	39964	39764	39768	40024
b8	40009	40165	39992	40134	39622	40003	40004	39786
c0	40249	40138	39942	39769	40128	40102	40137	39981
c8	39871	40051	40108	40271	39939	39861	40140	39746
d0	39862	40207	40321	40098	40077	39891	40222	39976
d8	40214	40013	39796	39759	40005	40068	40297	40041
e0	40087	40096	39795	39907	40001	40004	39893	39863
e8	40131	39859	40009	39923	40387	40240	39772	40142
f0	40022	39975	39517	40120	39777	40274	39932	40115
f8	40197	39827	40276	40039	40152	39947	39893	39983

Evaluation of count of 10240000 Bytes = 81920000 Bits:

Theoretical average of byte-frequencies: 40000  
'3c' = 39457 (minimum) '29' = 40528 (maximum)

Theoretical interval I of byte-frequencies:  
I = (39609 to 40391) (for 95 % of 256 frequency)

Test 1:

The theoretical permissible number of the 5% outliers (average 13) from the interval I is between 6 and 20

The real number of the outliers from interval I:  
smaller: 6 greater: 6 summary: 12

Test 2:

Evaluation of byte-frequencies  
Chi-square non-overlapping:  
Theoretical maximum chi-square = 293.25

Chi-square value = 244.14

Chi-square overlapping:

Theoretical maximum chi-square = 155.40

Chi-square value = 153.62

Test 3:

r = 0.49990565 (relative frequency of bit 1 in the bit stream)

For a truly random sequence, the probability for r to have values in the complement of the open interval (0.49990565 , 0.50009435) is  $w = 0.08763766$ .

If w is very small (e.g.,  $w < 0.05$ ), the null-hypothesis is rejected.

If more sequences can be tested, the probability w has to be  $\geq 0.05$  for about 95% of the tested bit sequences.

Test 4:

Frequencies of overlapping 2-tuples:

tuples 00: 20488614      tuples 01: 20479116

tuples 10: 20479115      tuples 11: 20473155

Check size: Chi-square of 2-bit patterns minus chi square of 1-bit patterns

Theoretical maximum chi-square = 5.99

Chi-square value = 3.07

Test 5:

Frequencies of 2-tuples on even places:

tuples 00: 10243019      tuples 01: 10242826

tuples 10: 10238865      tuples 11: 10235290

Theoretical maximum chi-square = 7.81

Chi-square value = 3.96

Test 6:

Frequencies of 2-tuples on odd places:

tuples 00: 10245595      tuples 01: 10236290

tuples 10: 10240250      tuples 11: 10237865

Theoretical maximum chi-square = 7.81

Chi-square value = 4.85

Result of statistical analysis of file txor31.rnd:

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The tests: 1 2 3 4 5 6 were fulfilled!

The null-hypothesis is accepted!